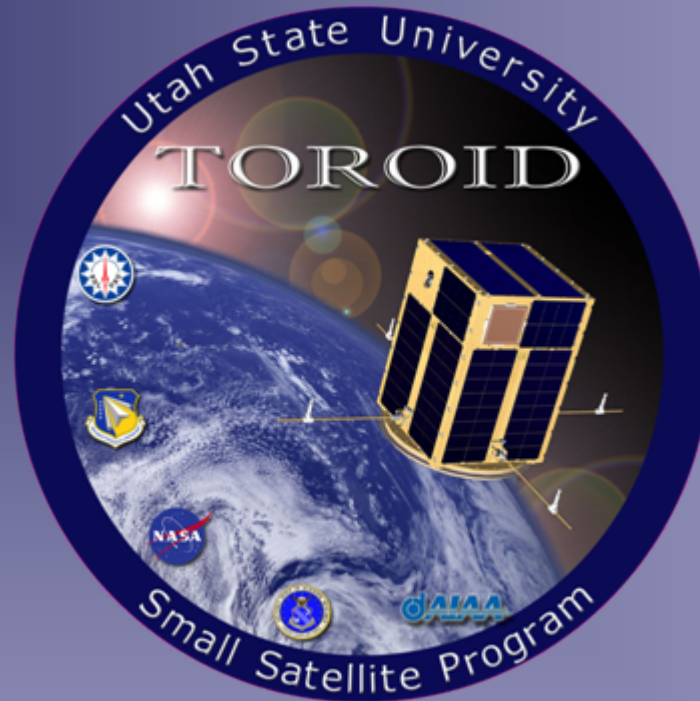


# USUSat III - TOROID

*TOmographic Remote Observer of Ionospheric Disturbances*



## Attitude Determination and Control

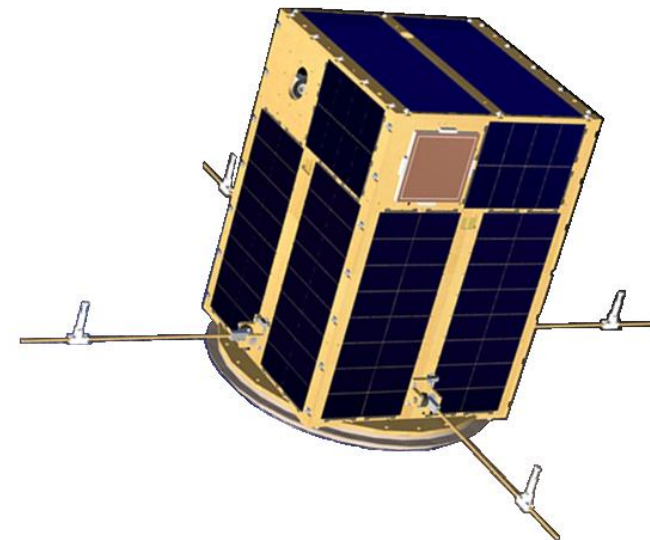
**UtahState**  
UNIVERSITY



## Attitude Determination and Control (ADC)

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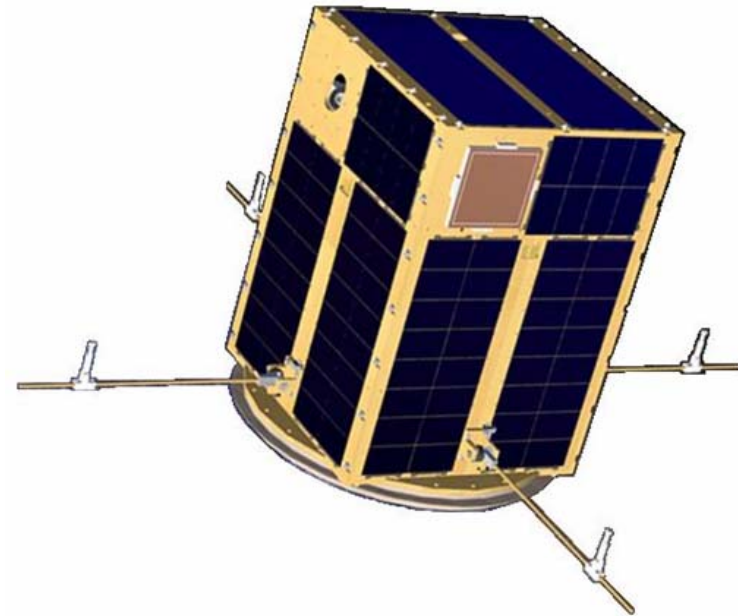
- Attitude
  - Orientation of the satellite relative to some reference frame (earth, stars, etc)
- Attitude Determination
  - Finding the current orientation of the spacecraft
- Attitude Control
  - Aligning the attitude of the satellite with a desired frame
- TOROID ADC Requirements
  - Without momentum bias:  $10^\circ$
  - With Momentum bias:  $1^\circ$



## Attitude Determination and Control Overview

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- Hardware and Restrictions
  - Attitude determination
    - Three-axis magnetometer
    - CMOS cameras
  - Attitude control
    - Torque coils
- ADC States
  - Detumble (2 phases)
  - Acquire attitude
  - Acquire control (with and without momentum bias)
- Linear Covariance Analysis

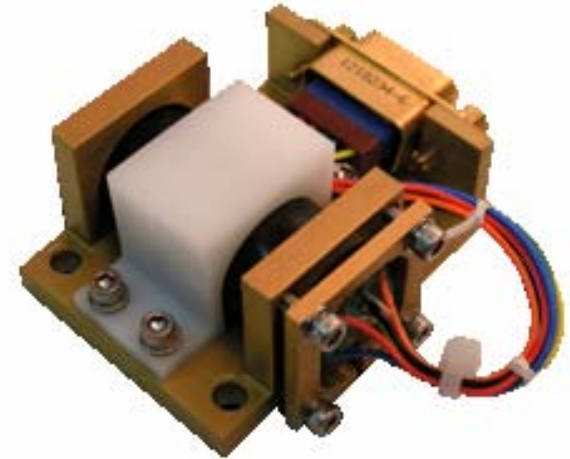


## Hardware: Attitude Determination Overview

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- Three-axis Magnetometer

- Measures direction and magnitude of the local magnetic field vector
- Will be the primary attitude determination hardware



- CMOS Cameras

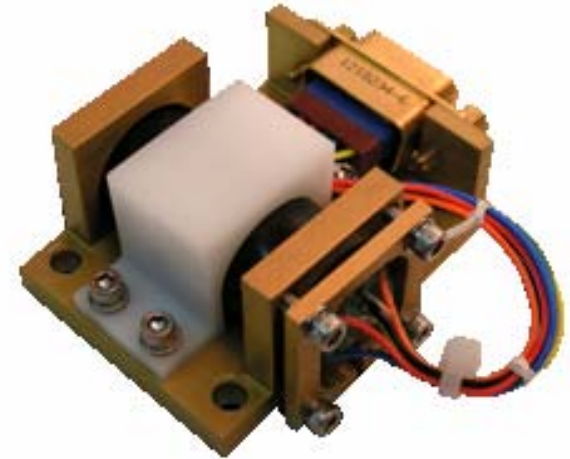
- Will be used to find the current sun vector and nadir vector
- Will significantly increase the accuracy of the attitude estimate



## Hardware: Attitude Determination Restrictions

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- Three-Axis Magnetometer
  - Sensitive to interference from the rest of the satellite
  - Requires accurate estimate of the expected local magnetic field vector

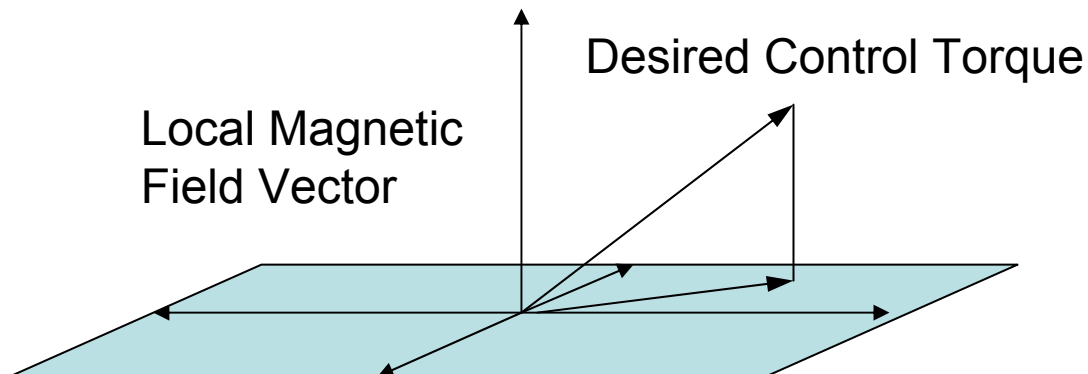


- CMOS Cameras
  - Only useful when the lighting conditions are good
  - Require image processing algorithms

## Hardware: Attitude Control Hardware and Restrictions

- Torque Coils
  - Rotate satellite using magnetic moments (like a compass pointing north)
- Restrictions:
  - The torques that can be generated are, by definition, in the plane perpendicular to the local magnetic field vector
  - The desired torque usually is not!
  - System is only controllable over time

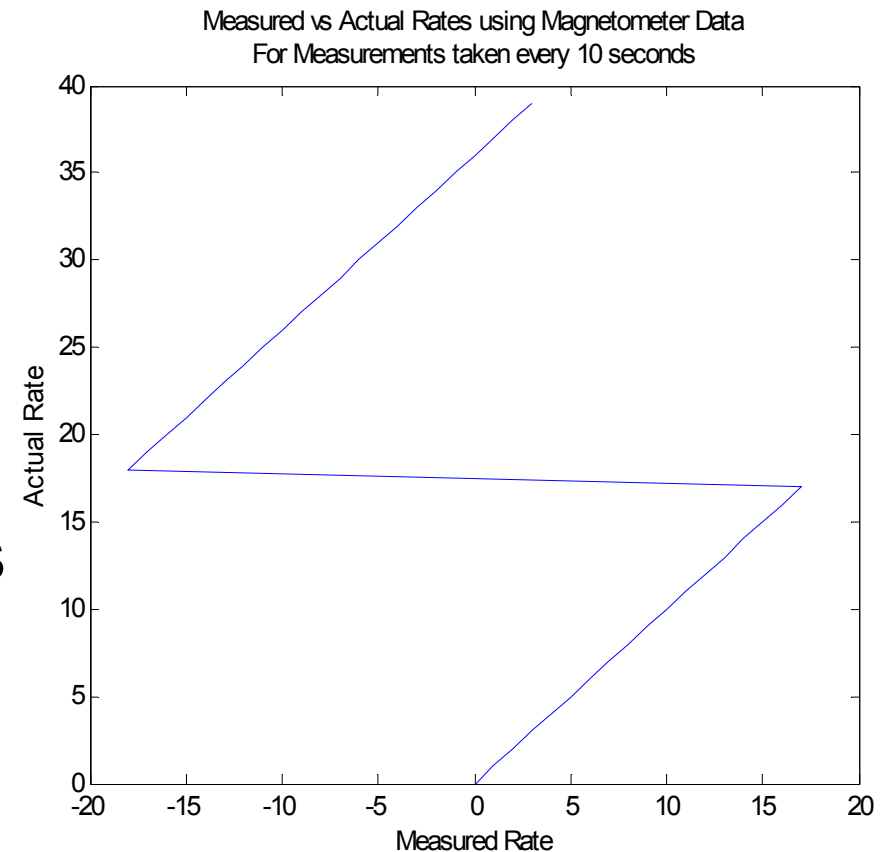
$$\bar{T} = \bar{b}(t) \times \bar{M}$$



## ADC States: Detumble-Phase 1

- **Spacecraft Initial Rates Reduction**

- Rates over  $180^\circ/\text{sec}$  are impossible to estimate (given TAM measurements every 10 seconds)
- Rate reduction by leaving the torque coils on (has same effect as a boom)
- Example: Alsat 1



## ADC States: Detumble-Phase 2

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- **Bdot: A Simple Algorithm for Rate Reduction**
  - The desired control torque is proportional to rate of change of the magnetic field vector

$$\mathbf{T}_c = \mathbf{K}\dot{\mathbf{B}}$$

- Guaranteed to reduce rates if a good estimate of the rate of change of the magnetic field vector is available
- Does nothing to correct attitude errors



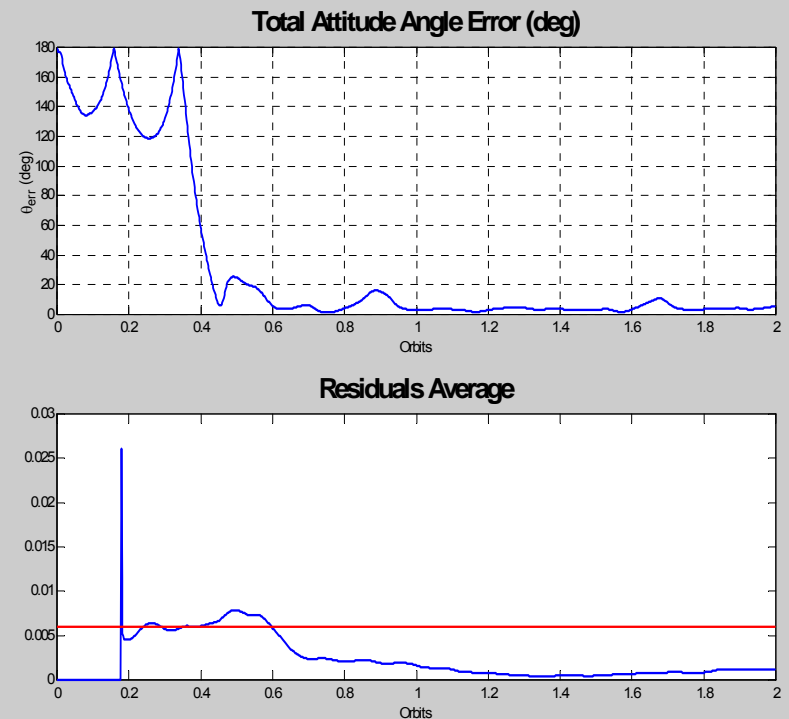
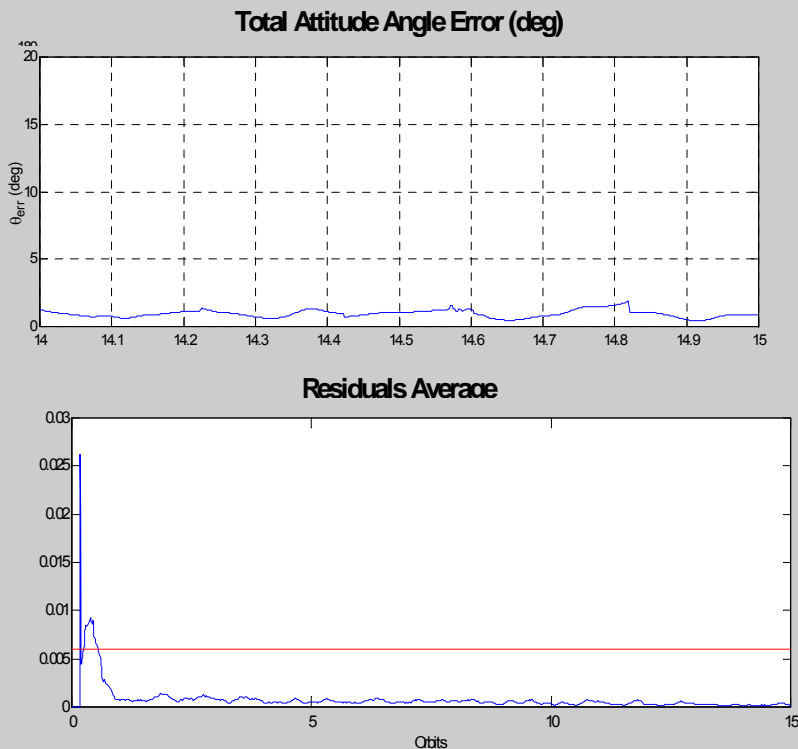
## ADC States: Acquire Attitude

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- Attitude Estimation: Adapted from ION-F
- State Estimation Kalman Filter
  - Estimates orientation, rates and disturbance torques
  - Expected error (using TAM only)
    - Attitude:  $4.8^\circ$  ( $3\sigma$ )
    - Rates:  $0.018^\circ/\text{sec}$  ( $3\sigma$ )
    - When sun and nadir vectors are available, attitude estimation error is less than  $0.5^\circ$
- Calibration Kalman Filters
  - CF1: Estimates non-orthogonality, bias, and scale factor errors (temperature dependant)
  - CF2: Estimates TAM orientation error
  - CF1 and CF2 can be enable/disabled automatically or using commands from the ground

## ADC States: Acquire Attitude

- Some Results: (Best) and (Worst) Case
  - Initial rates: (0 deg/s) and (1 deg/s)
  - Initial orientation: (0 deg) and (180 deg)



## ADC States: Acquire Control (Controller Design)

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- LQ Regulator (for  $T_c$ =control torques and  $B$ =measured magnetic field vector)
  - $\mathbf{x}$ =Euler angles

$$T_c = G(t)K \begin{bmatrix} \int \mathbf{x} \\ \mathbf{x} \\ \dot{\mathbf{x}} \end{bmatrix}$$

Where  $\mathbf{K}$  is the controller Gain and

$$G(t) = \frac{-I^{-1}}{\|B\|} [B \times] [B \times] = \frac{I^{-1}}{\|B\|} \begin{bmatrix} B_y^2 + B_z^2 & -B_x B_y & -B_x B_z \\ -B_x B_y & B_x^2 + B_z^2 & -B_y B_z \\ -B_x B_z & -B_y B_z & B_x^2 + B_y^2 \end{bmatrix}$$

## ADC States: Acquire Control (Controller Design)

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- Gain Selection

$$K = -R^{-1}\bar{G}^T P$$

$\bar{G}$  is the time average of  $G(t)$  over a single orbit  
and  $P$  comes from the steady state solution to the Riccati Equation:

$$\dot{P} + PF + F^T P - P\bar{G}R^{-1}\bar{G}^T P + Q = 0$$

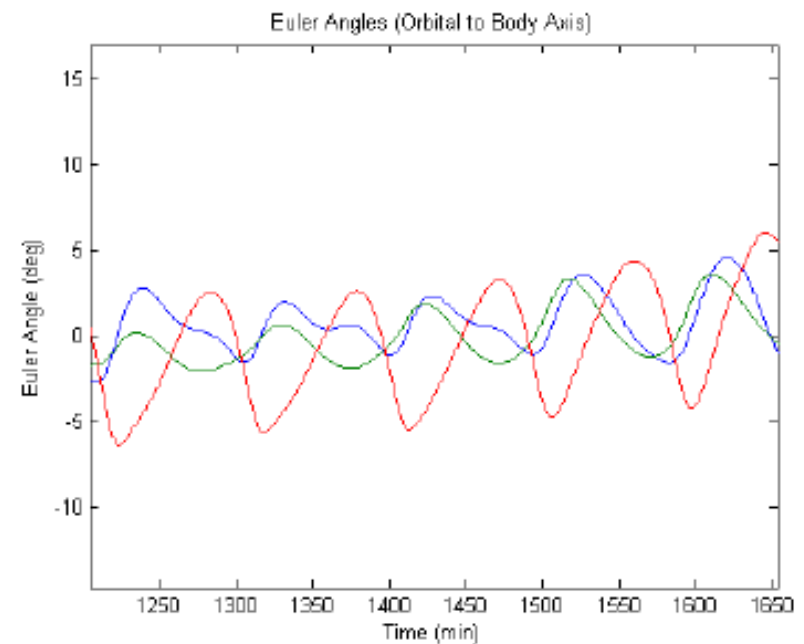
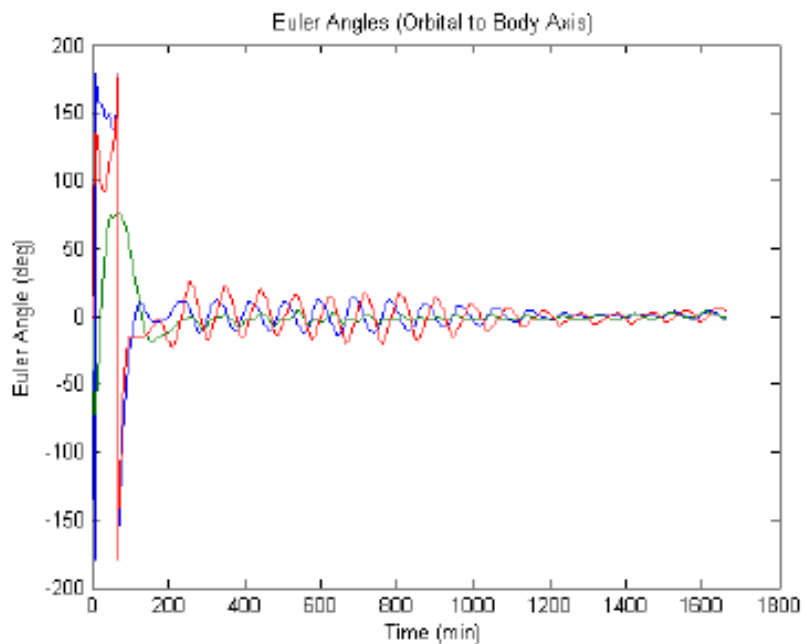
$Q$  and  $R$  are chosen according to the desired response of the system.

Note:  $K$  is optimal, given  $Q$  and  $R$ ; however, there is no method for finding the optimal  $Q$  and  $R$



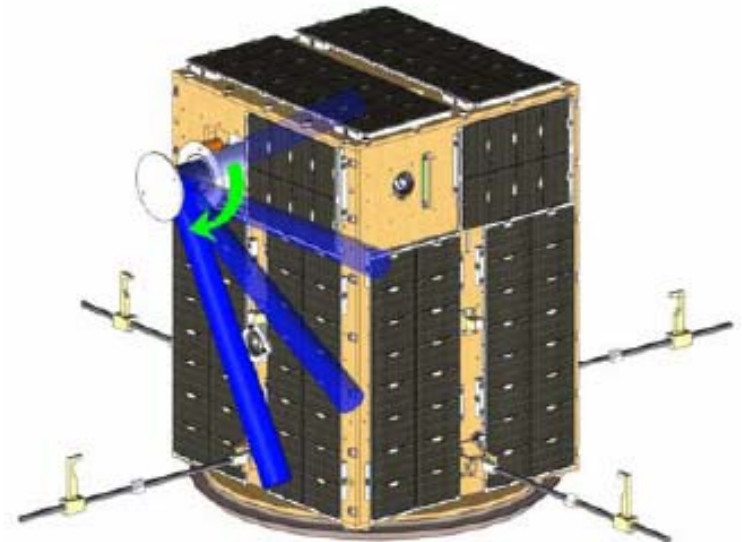
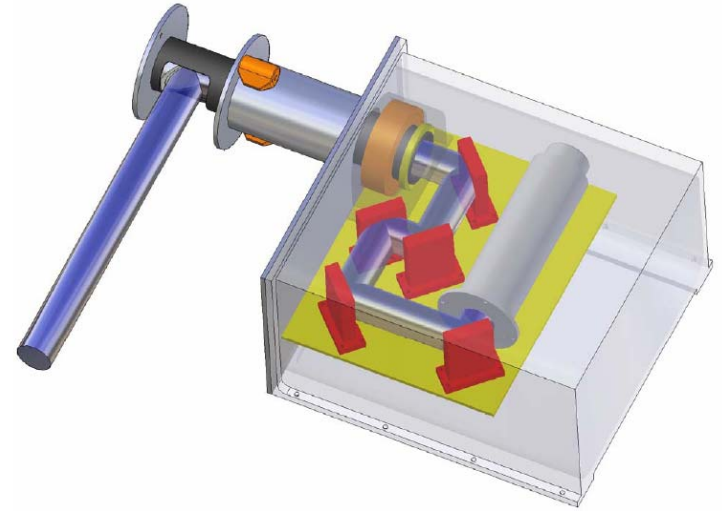
## ADC States: Acquire Control (No Momentum bias)

- Sample Results: Altitude=350 km and  $i=51^\circ$ 
  - Able to meet mission requirements even if the CMOS data (sun and nadir vectors) are not available



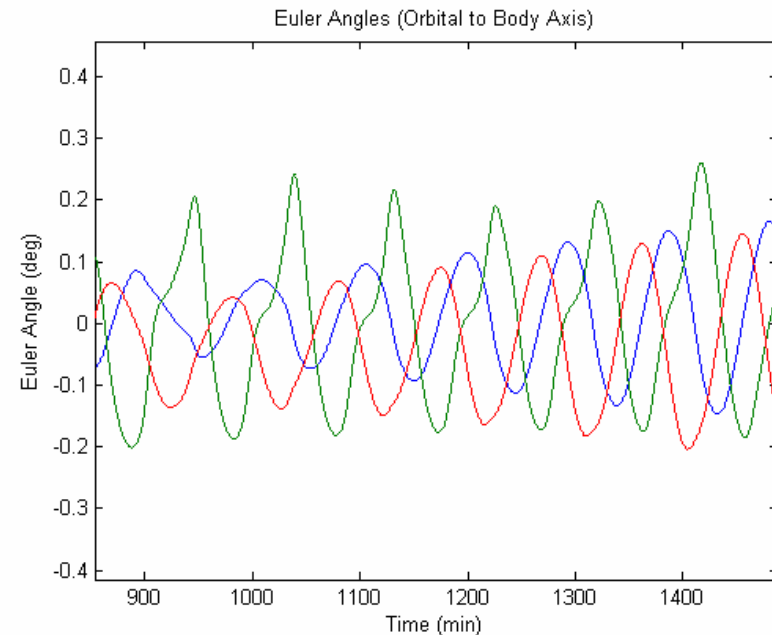
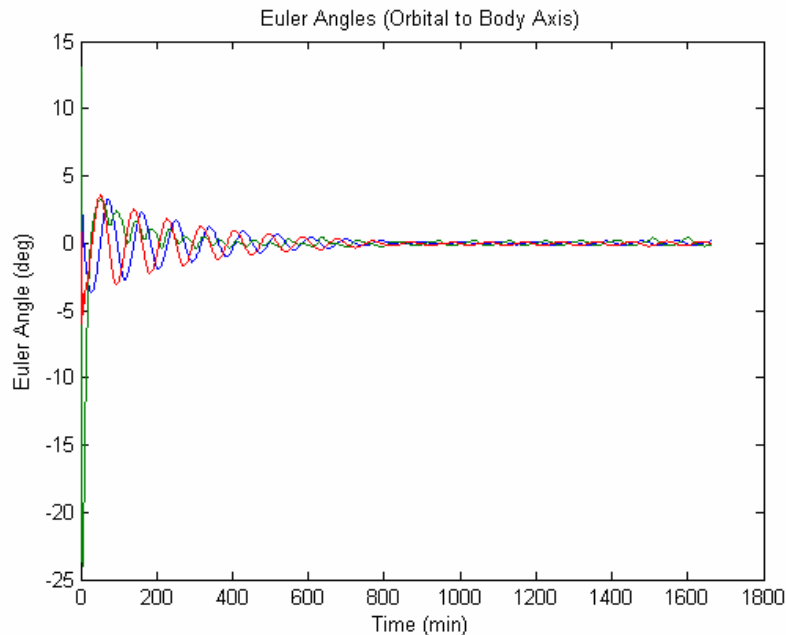
## ADC States: Spinup

- As the Science Instrument Spins up:
  - The acceleration of the instrument causes the rest of the spacecraft to accelerate in the opposite direction about the y axis
  - The increase in total momentum adds helps stabilize the satellite about the x and z axes



## ADC States: Acquire Control (With Momentum bias)

- Sample Results:  $H_w = 0.05 \text{ Nms}$ ,  $a=350$ ,  $i=51^\circ$ 
  - Meets science mission requirements assuming:
    - CMOS measurements are available
    - sufficient momentum bias.



## Linear Covariance Analysis

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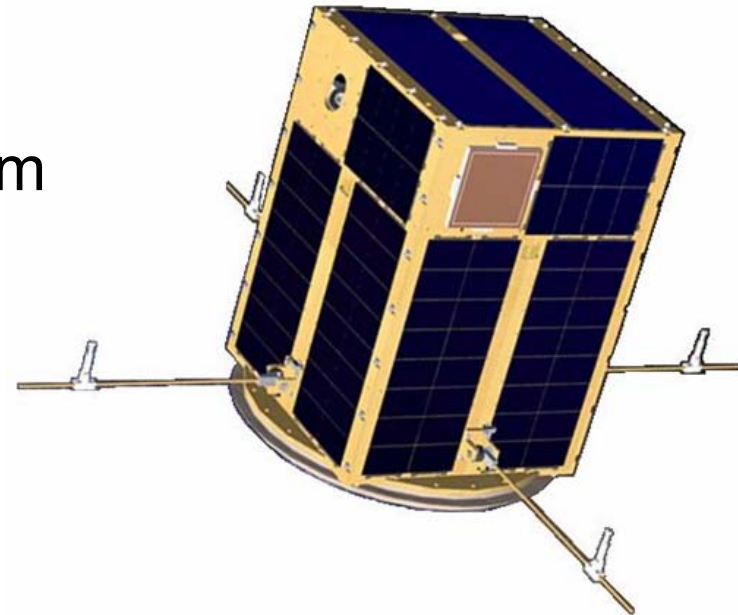
- Linear Covariance (Only for ADC with Momentum bias)
  - Nonlinear system can be described by a set of linear equations written as a stochastic process description (Maybeck 1978)
  - Allows a single simulation run to generate Monte Carlo-type information
  - Possible inputs to vary: science instrument misalignment, sensor biases, sensor noise, orbit parameters, TLE accuracy
  - Desired results: expected error and sensitivity to changes in inputs



## ADCS States: General Notes

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- Control is Robust:
  - High and low inclination controller gains are saved onboard
  - New gain (optimized for a particular orbit) can be sent from ground station
- Control not Optimal
- Achieving Science Mission Requirements
  - Only possible with CMOS measurements.
  - For the ION-F mission, these measurements are not available when we need them.



## ADC: To Do and Future Work

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- To Do for TOROID
  - Magnetic interference testing
  - Increase momentum from science instrument (increase speed or add mass)
  - Image processing
  - Final testing and analysis
- Future Work at USU
  - Attitude determination
    - Infrared horizon sensing
    - Star Tracking with CMOS cameras
  - Control
    - Time varying
    - Optimal

